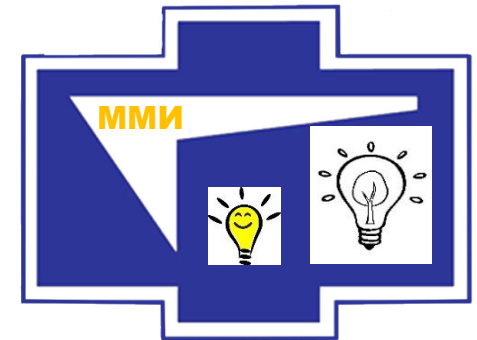


# Оценивание параметров кильватерных следов кораблей, вихрей, пожаров в дистанционных исследованиях

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[en.teren@mail.ru](mailto:en.teren@mail.ru); [en.teren@physics.msu.ru](mailto:en.teren@physics.msu.ru);

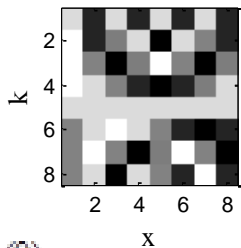


The image is associated with its vector gradient field. The analysis of vector fields with the help of single-length vector templates made it possible to localize (indicate) object in the image by calculating the main parameters of the object: position and size. The proposed method of indicating local objects using gradient fields turned out to be highly precision and noise-immunity.

# 1D FDST in mathematical analysis

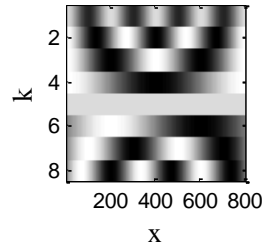
Theorem (Terentiev): 3 objects are given: an array (row) of samples  $D=f(x_0)$  and two matrices: Fourier harmonics  $H^{(0)}(x_0)$ ,  $x_0=0 : N-1$  и  $H^{(n)}(x)$ ,  $x=0 : dx : N-dx$ , then the “continuous” function  $dx < 1$   $f^{(n)}(x) = (H^{(0)}(x_0) * D)' * H^{(n)}(x)$  for  $n = 0$  passes through the samples points  $D=f(x_0)$ .

Fourier harmonics



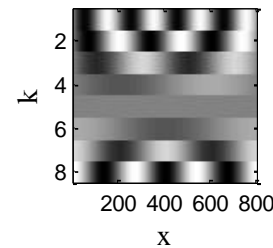
$$H^{(0)}(x_0), N=8, dx=1$$

Interpolation



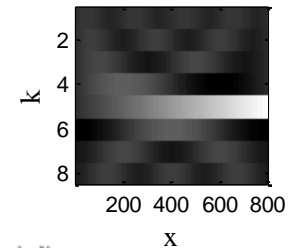
$$H^{(0)}(x), N=8, dx=0.01$$

Differentiation



$$H^{(1)}(x), N=8, dx=0.01$$

Integration



$$H^{(-1)}(x), N=8, dx=0.01$$

In  $f^{(n)}(x)$  the first asterisk implements the direct Fourier Transform with harmonics  $H^{(0)}(x_0)$ ,  $dx=1$  and the second asterisk implements the inverse FT with  $H^{(n)}(x)$ ,  $dx < 1$ .

For  $n > 0$ , we realize the  $n$ -th order derivative, and for  $n < 0$ , the  $-n$  order integral with the result in the form of an interpolated “continuous” function with digitization step  $dx < 1$ .

# 3D FDST in field theory operations

Theorem (Terentiev): 3 objects are given: an array of samples  $D=f(x_0, y_0, z_0)$ , the matrices are the Fourier harmonics  $H^{(0)}(x_0)$ ,  $x_0=0 : N-1$  and  $H^{(n)}(x)$ ,  $x=0 : dx : N-dx$ , then the “continuous” function ( $dx < 1$ )

$$f^{(nx, ny, nz)}(x, y, z) = \sum_{k_x, k_y, k_z=1}^N c_{k_x, k_y, k_z} * H^{(n_x)}(k_x, x) * H^{(n_y)}(k_y, y) * H^{(n_z)}(k_z, z), \quad (1)$$

$$\begin{aligned} c_{k_x k_y k_z} &= (f(x_0, y_0, z_0), H^{(0)}(k_x, x_0) * H^{(0)}(k_y, y_0) * H^{(0)}(k_z, z_0)) = \\ &= \sum_{x_0, y_0, z_0=1}^N f(x_0, y_0, z_0) * H^{(0)}(k_x, x_0) * H^{(0)}(k_y, y_0) * H^{(0)}(k_z, z_0), \quad k_x, k_y, k_z = 1 : N. \end{aligned} \quad (2)$$

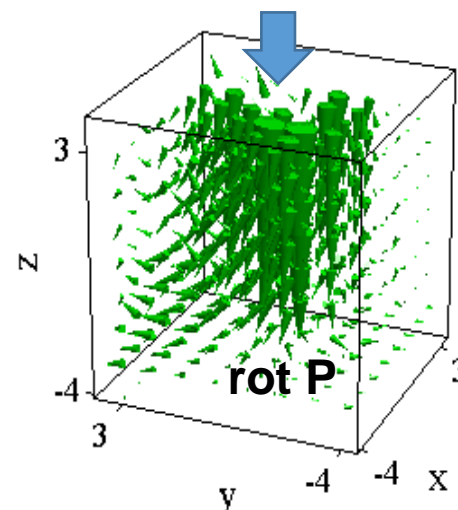
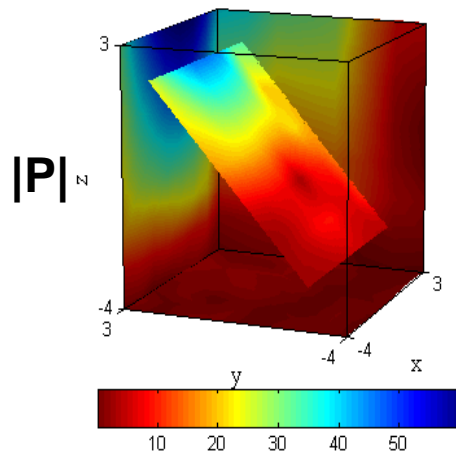
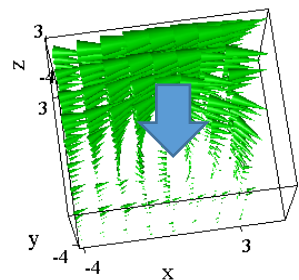
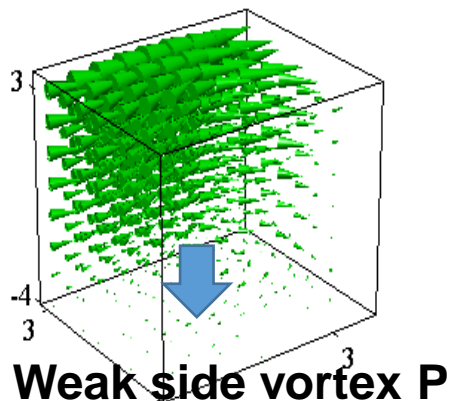
passes through sampling points  $f^{(nx, ny, nz)}(x_0, y_0, z_0)$ .

Scalar products (2) are realized by direct FT, and the Fourier series (1) is realized by “invers FT” with interpolation if  $dx < 1$ .

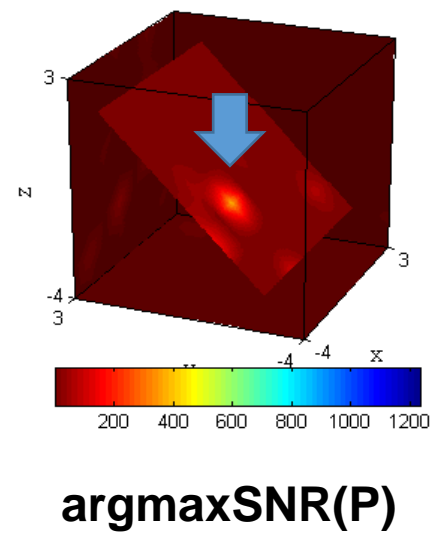
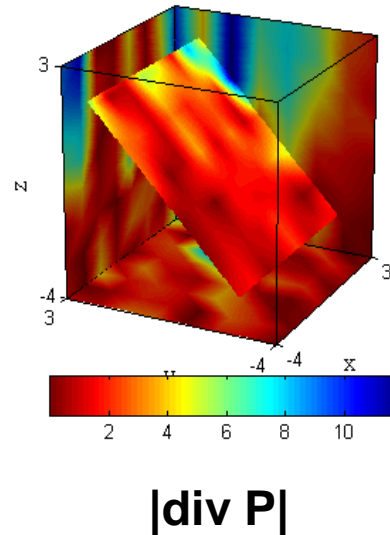
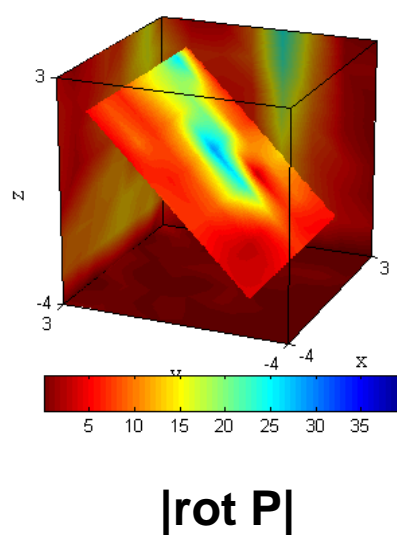
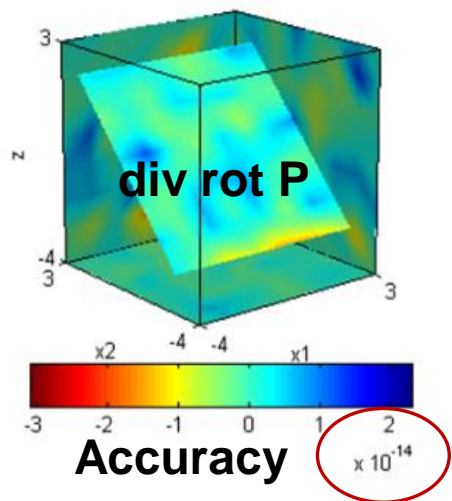
The gradient of the array of numbers  $D=f(x_0, y_0, z_0)$ :

$$\text{grad } D(x, y, z) = \left\{ \frac{\partial}{\partial x} D, \frac{\partial}{\partial y} D, \frac{\partial}{\partial z} D, \right\} = \{ f^{(1,0,0)}(x, y, z), f^{(0,1,0)}(x, y, z), f^{(0,0,1)}(x, y, z) \}$$

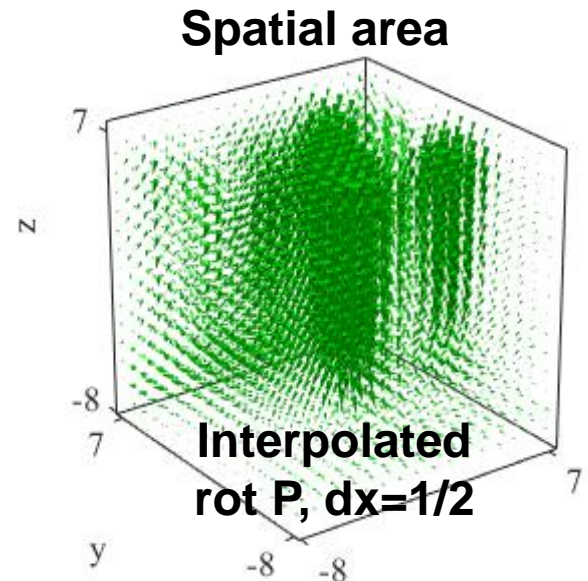
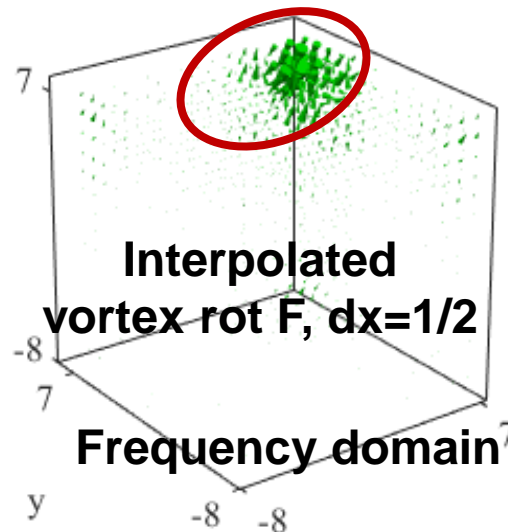
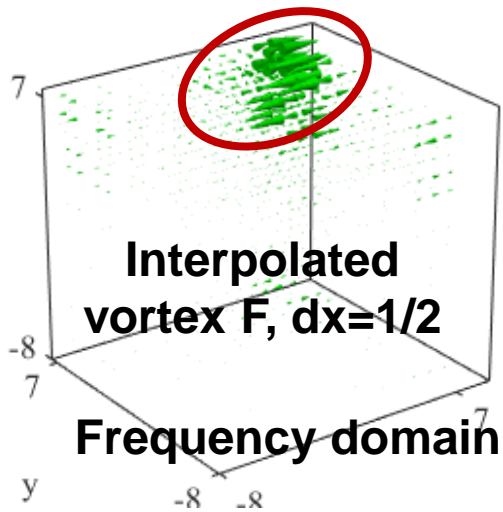
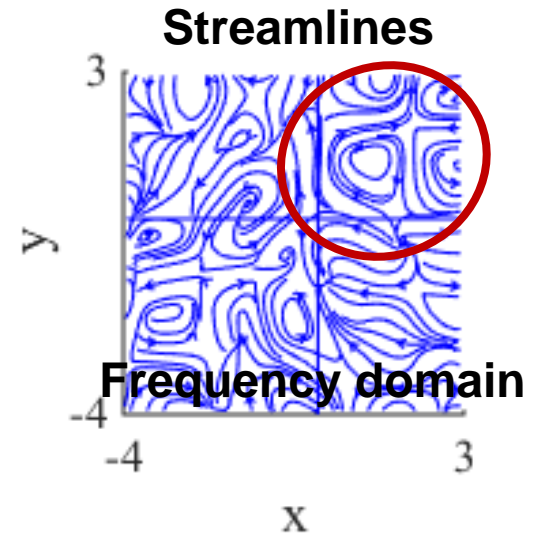
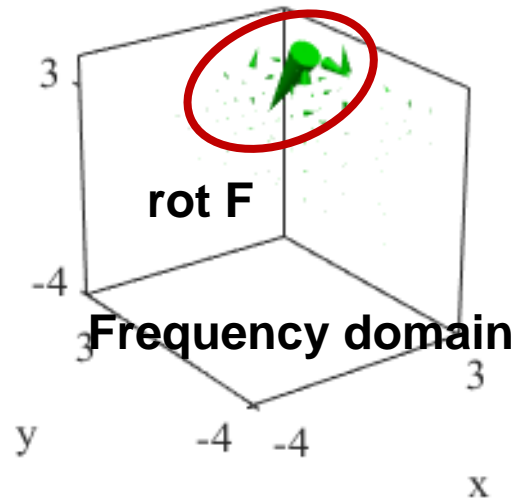
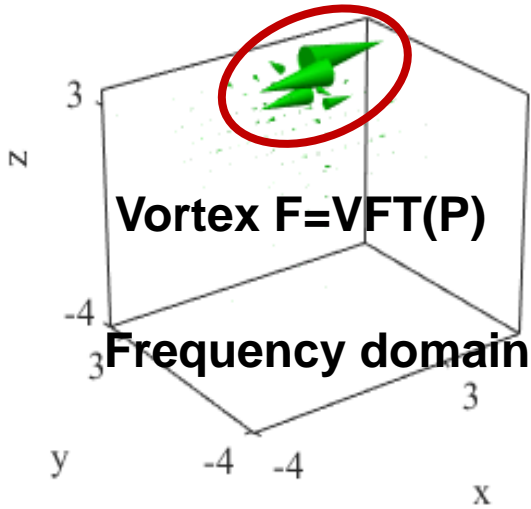
# Localization of the vortex with its axis of rotation



$$\text{SNR}(P) = |\text{rot } P| / |\text{div } P|$$



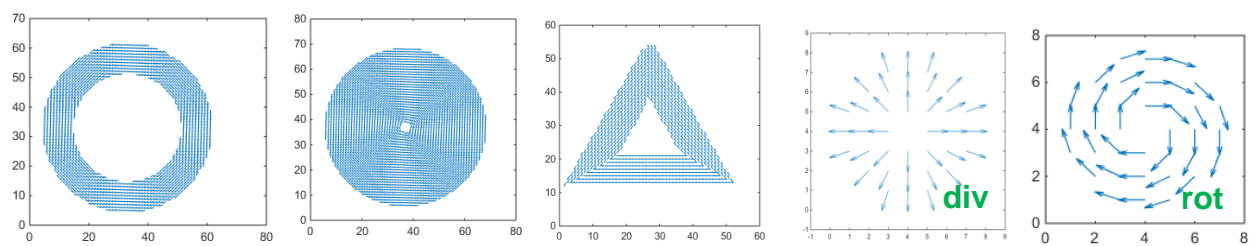
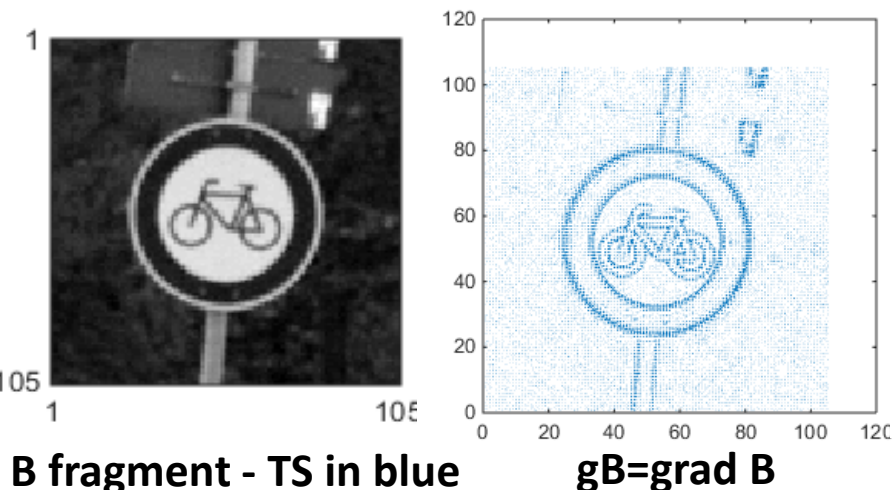
# Interpolations and vortices in the frequency domain



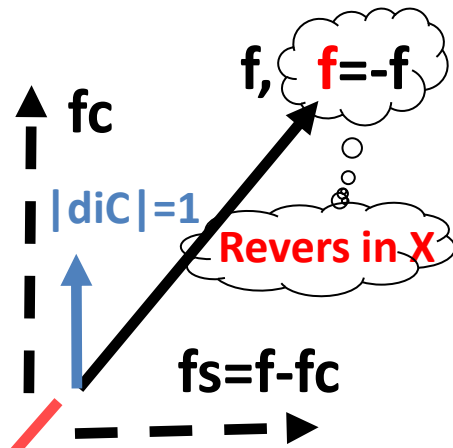
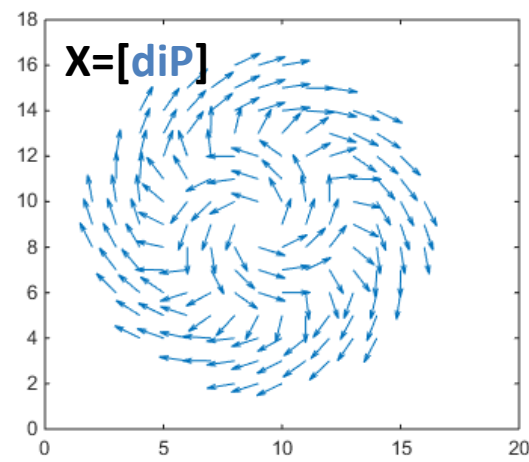
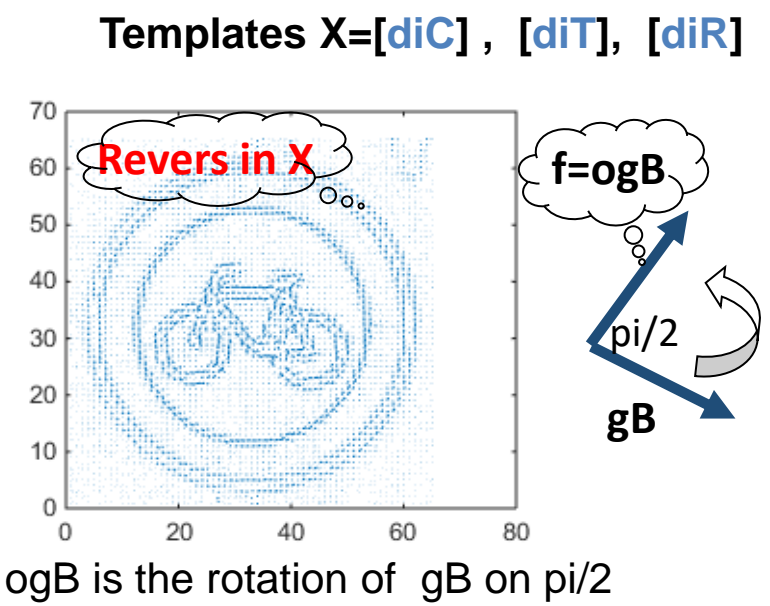
# The main the concepts

$$\text{SNR}(f|X) = [f_c]^2 / [f_s]^2$$

$$\text{aSNR}(f|X) = \text{atan2}([f_c], [f_s])$$



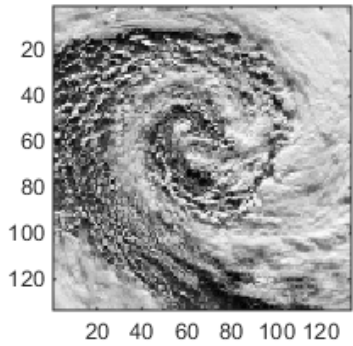
Projections  $f_c$  and  $f_s$  on  $diC$  direction,  $X = [diC]$



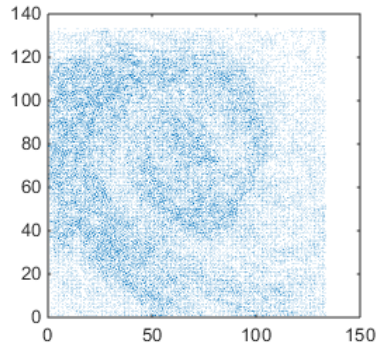
**Object coordinates  $(x_o, y_o) = \text{argmaxSNR}(f|X)$ , by  $(x, y)$  from  $S$  - scanning area by template  $X$**



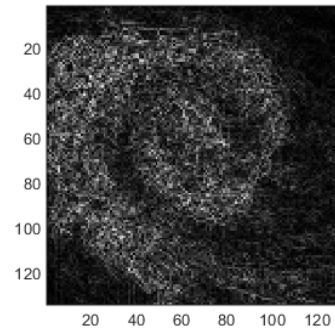
# Vortices in space images



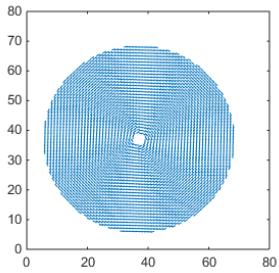
Vortex B



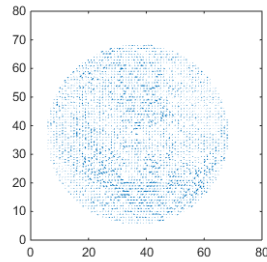
$gB = \text{grad } B, f = \text{og}B$



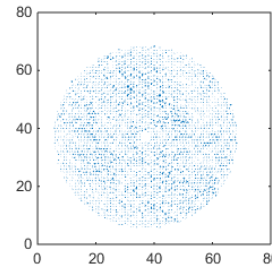
$|gB| = |\text{og}B|$



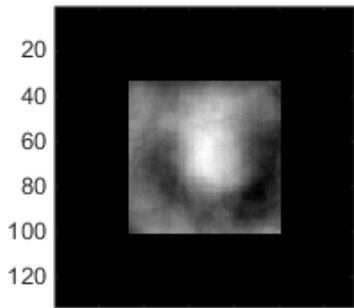
Template = [diC]



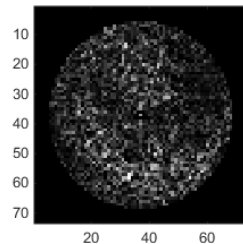
Signal fc



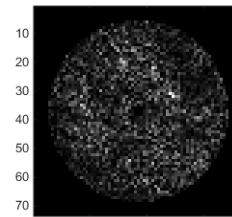
Noise fs



SNR(ogB|X) in S



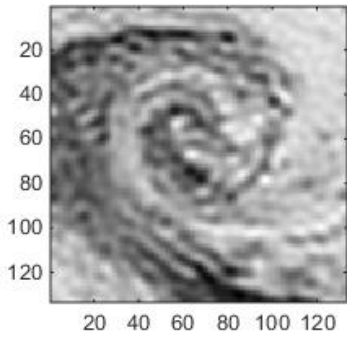
$|fc|$



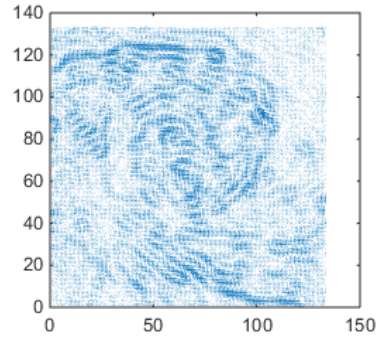
$|fs|$

**In 100%  
frequency  
band**

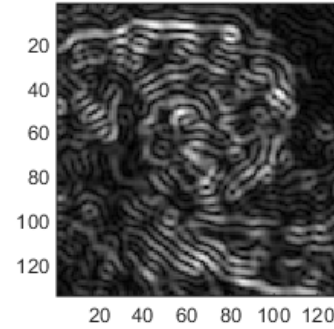
# Vortices in space images



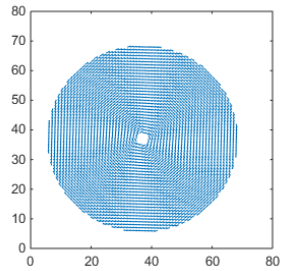
30% LF B



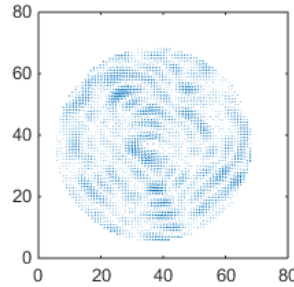
$gB = \text{grad } B, f = \text{og}B$



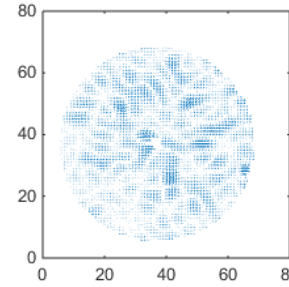
$|gB| = |ogB|$



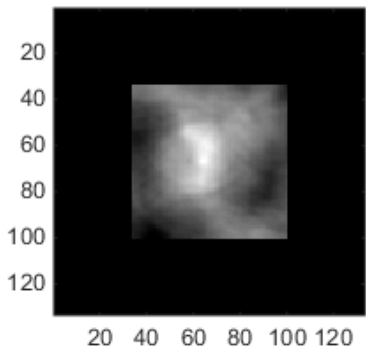
Template  $X = [diC]$



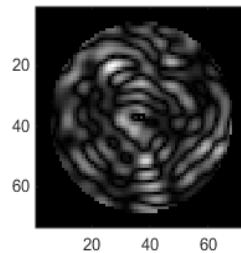
Signal  $fc$



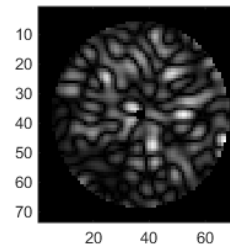
Noise  $fs$



$\text{SNR}(\text{og}B|X) \text{ in } S$



$|fc|$

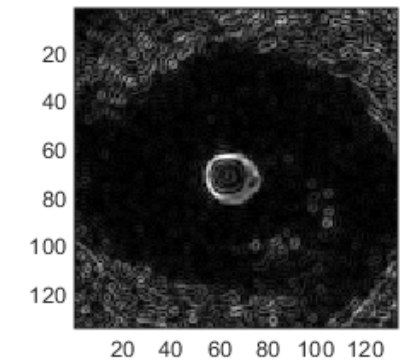
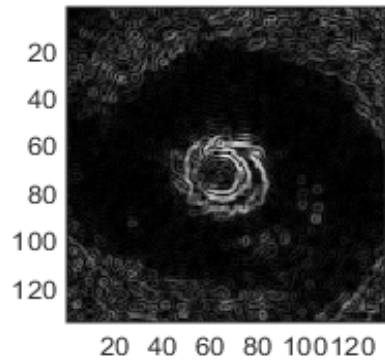
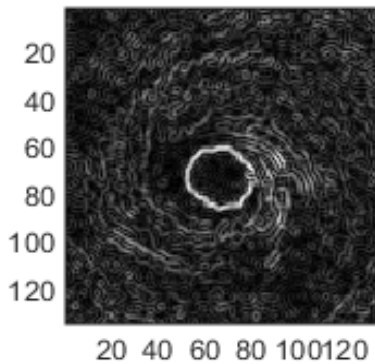
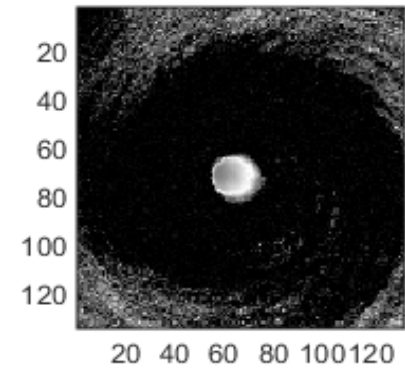
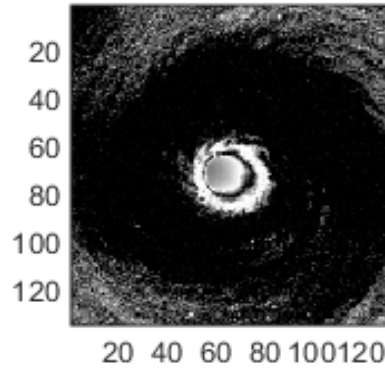
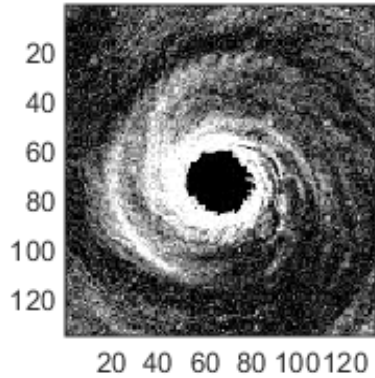
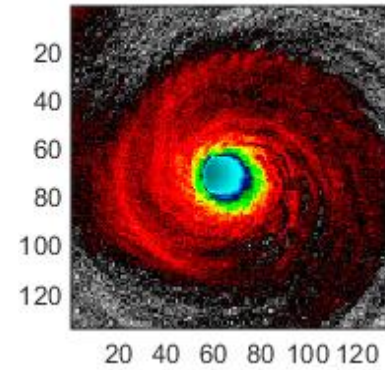
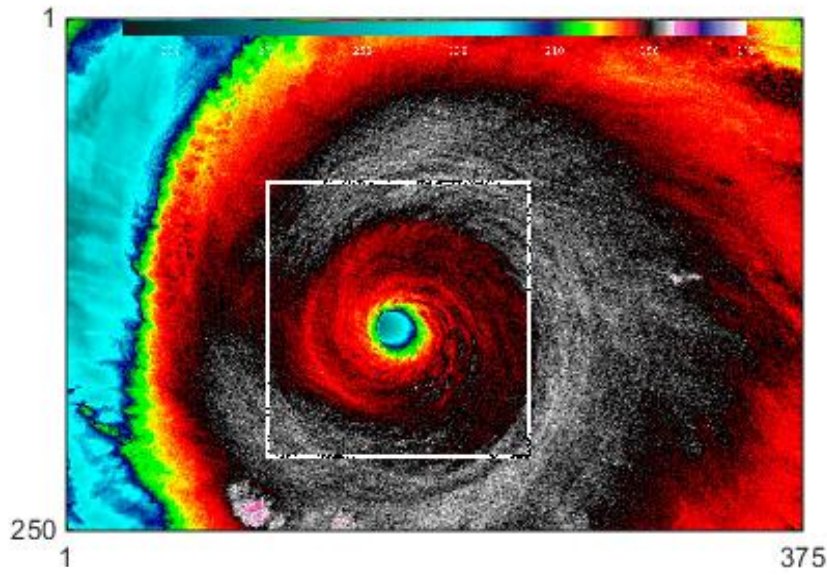


$|fs|$

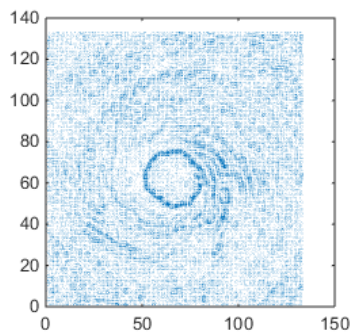
**30% Low  
Frequency B**



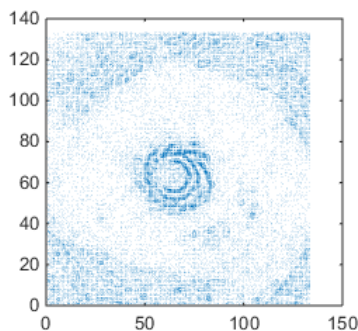
# Vortices in IR space images



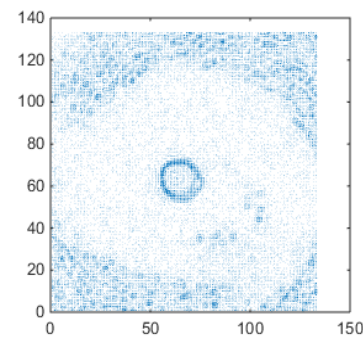
# Parameters of vortices in **IR** space images



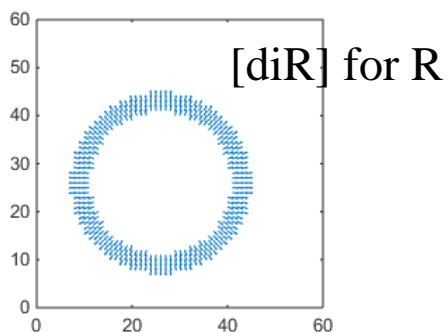
gR



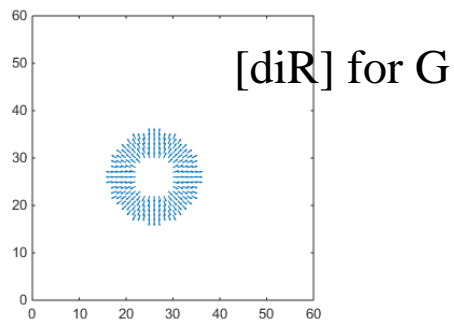
gG



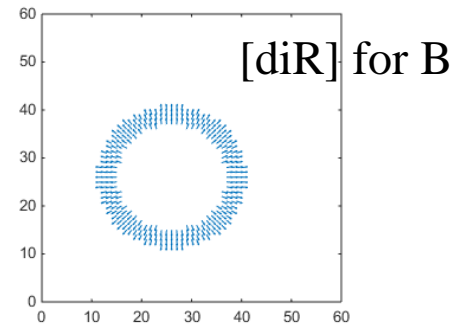
gB



[diR] for R

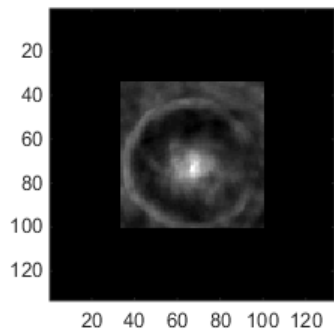


[diR] for G

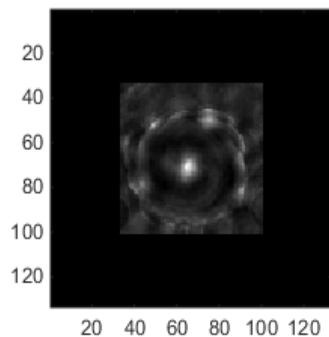


[diR] for B

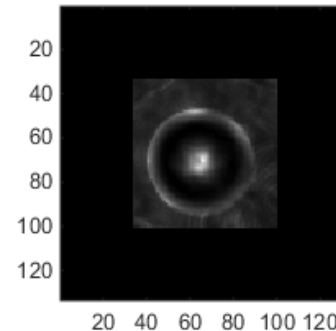
maxSNR~2.64



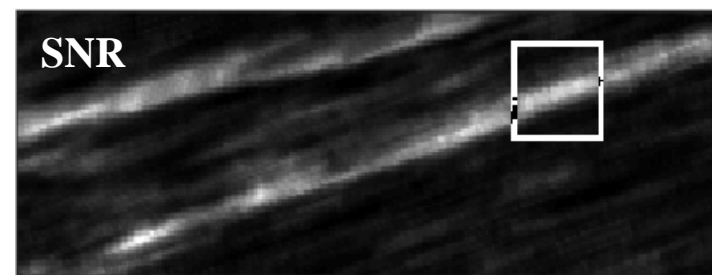
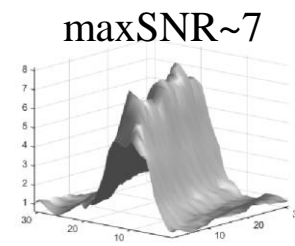
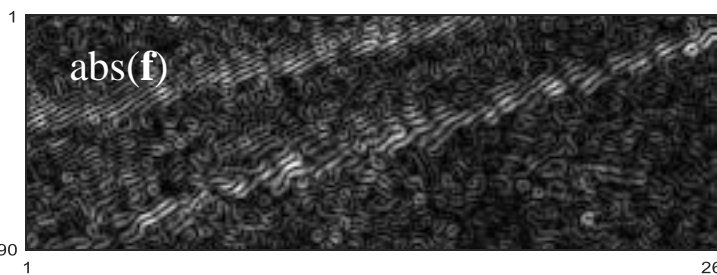
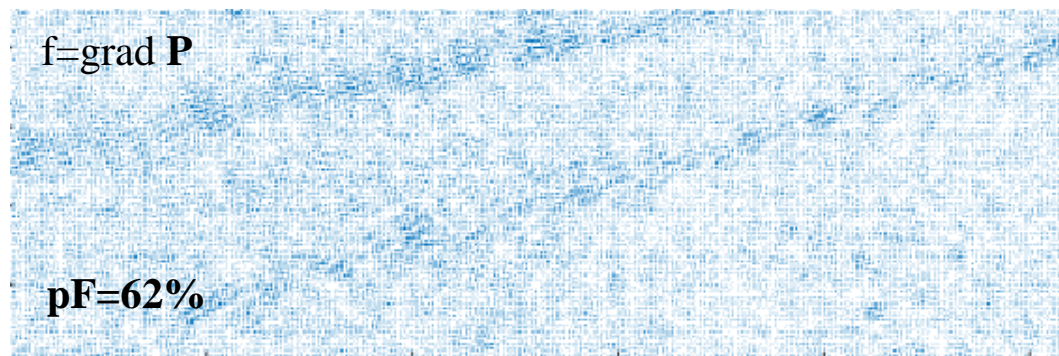
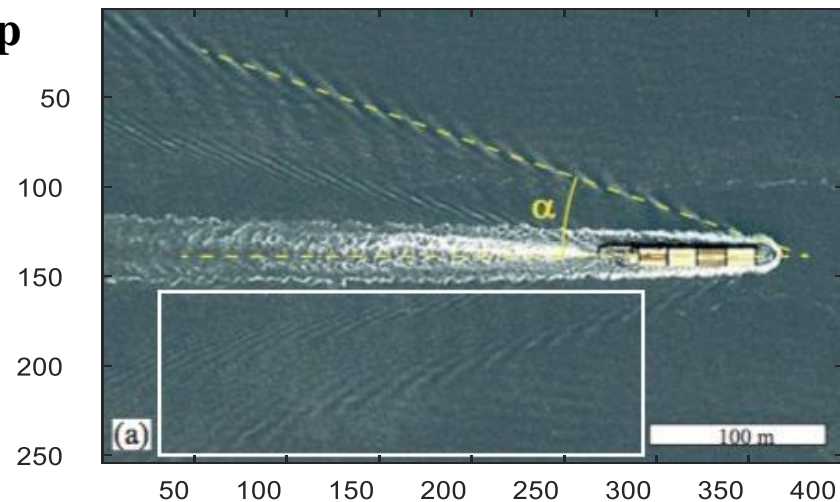
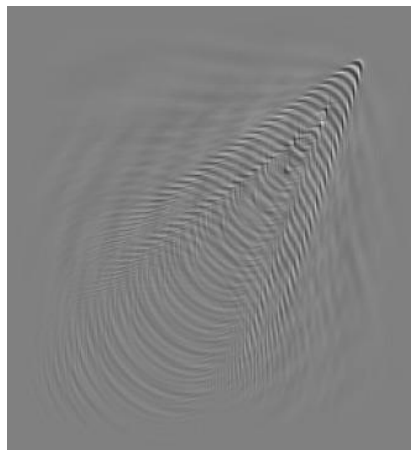
maxSNR~3.51



maxSNR~5.46

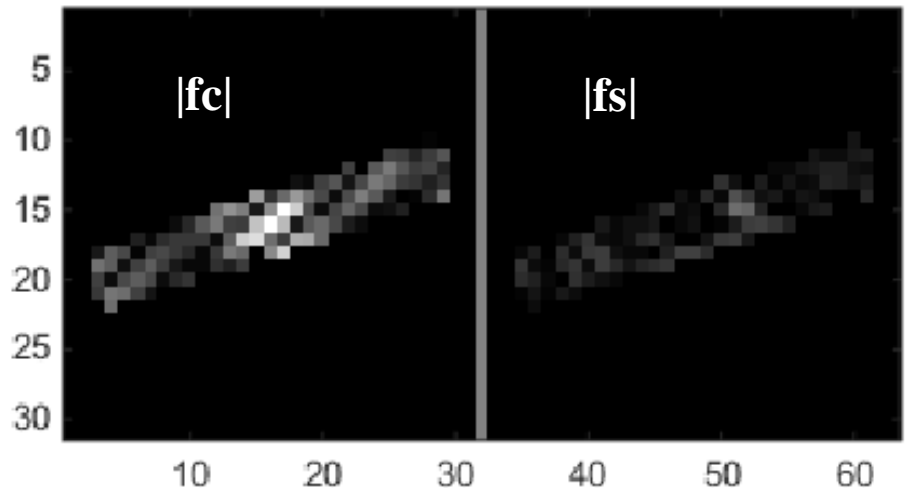
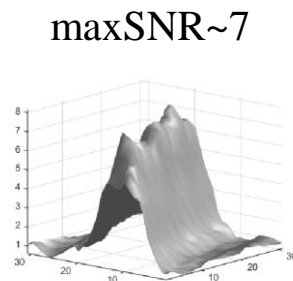
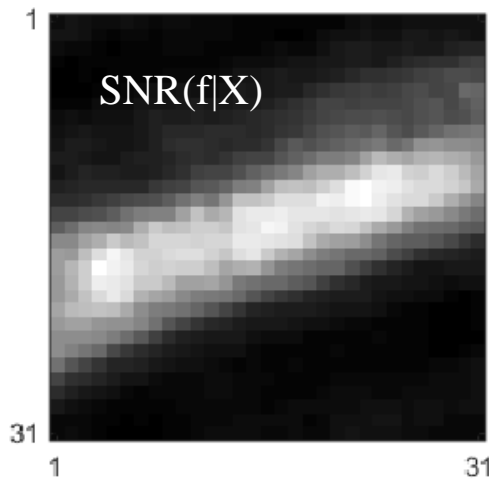
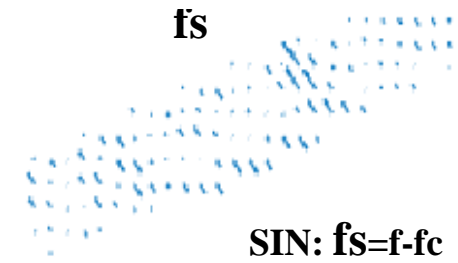
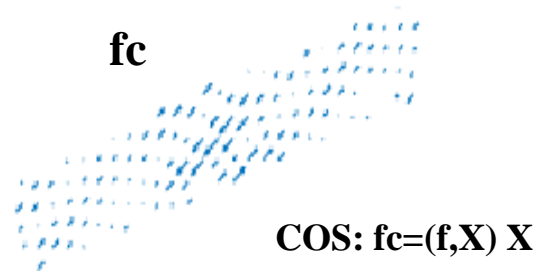
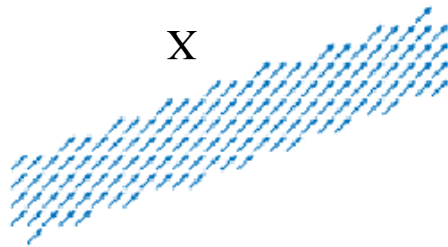
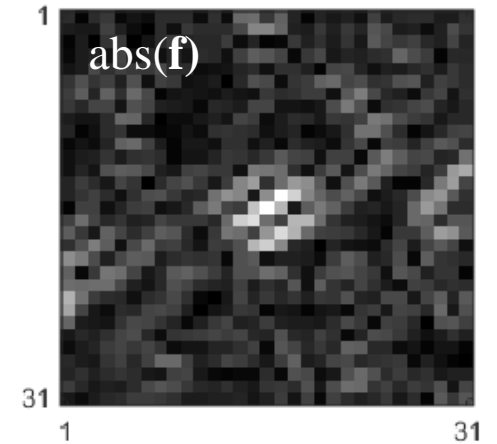
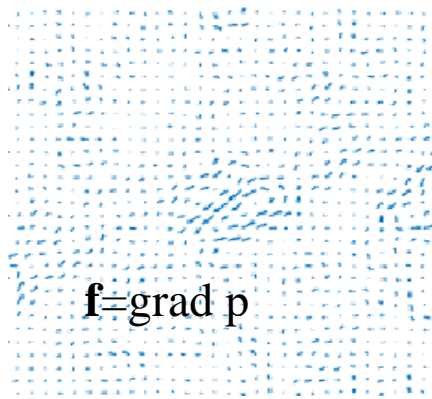
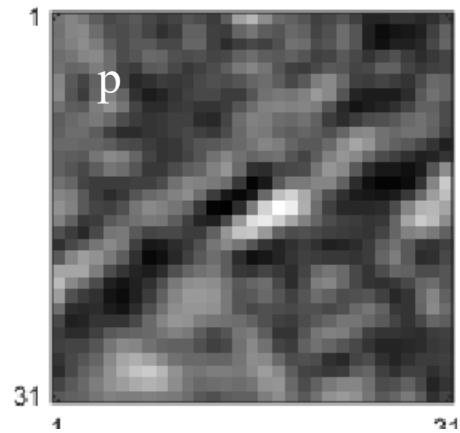


# Parameters of the shape of the wakes and parameters of the shape of the boundaries of the plume of the ship

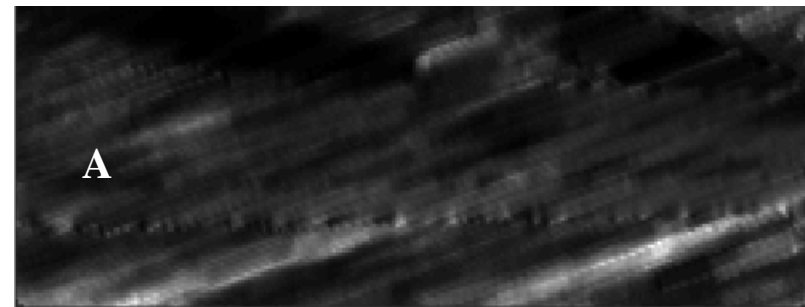
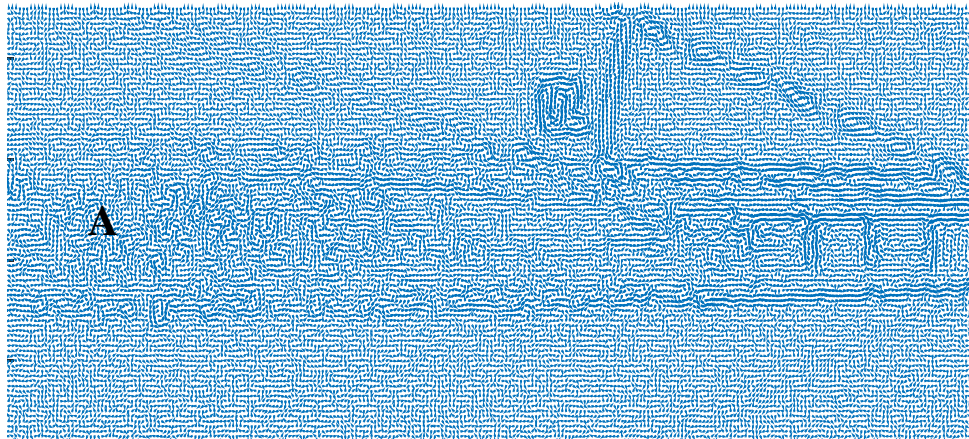
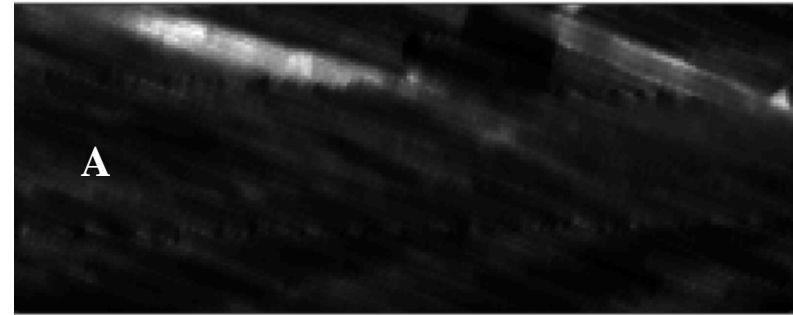
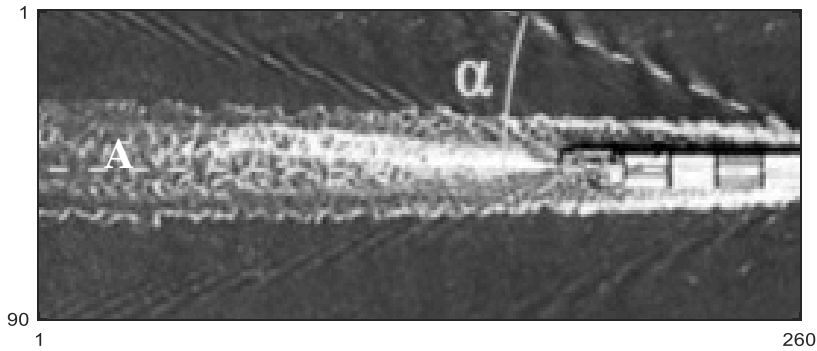




# Ship wake parameters

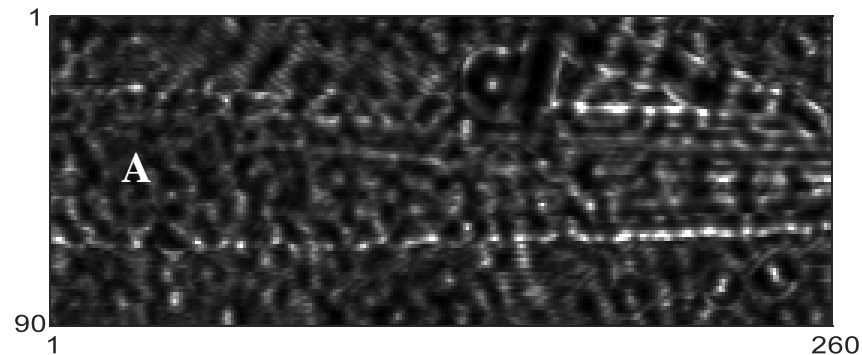
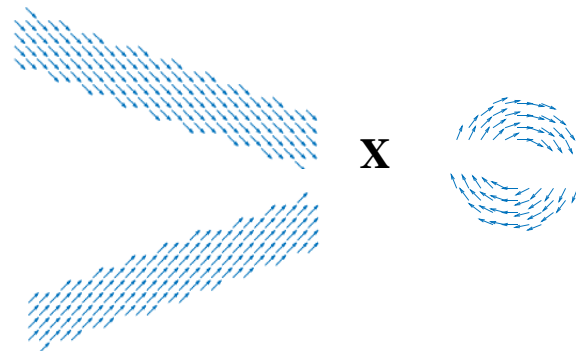


# Templates X for wakes and turbulent plume of the ship

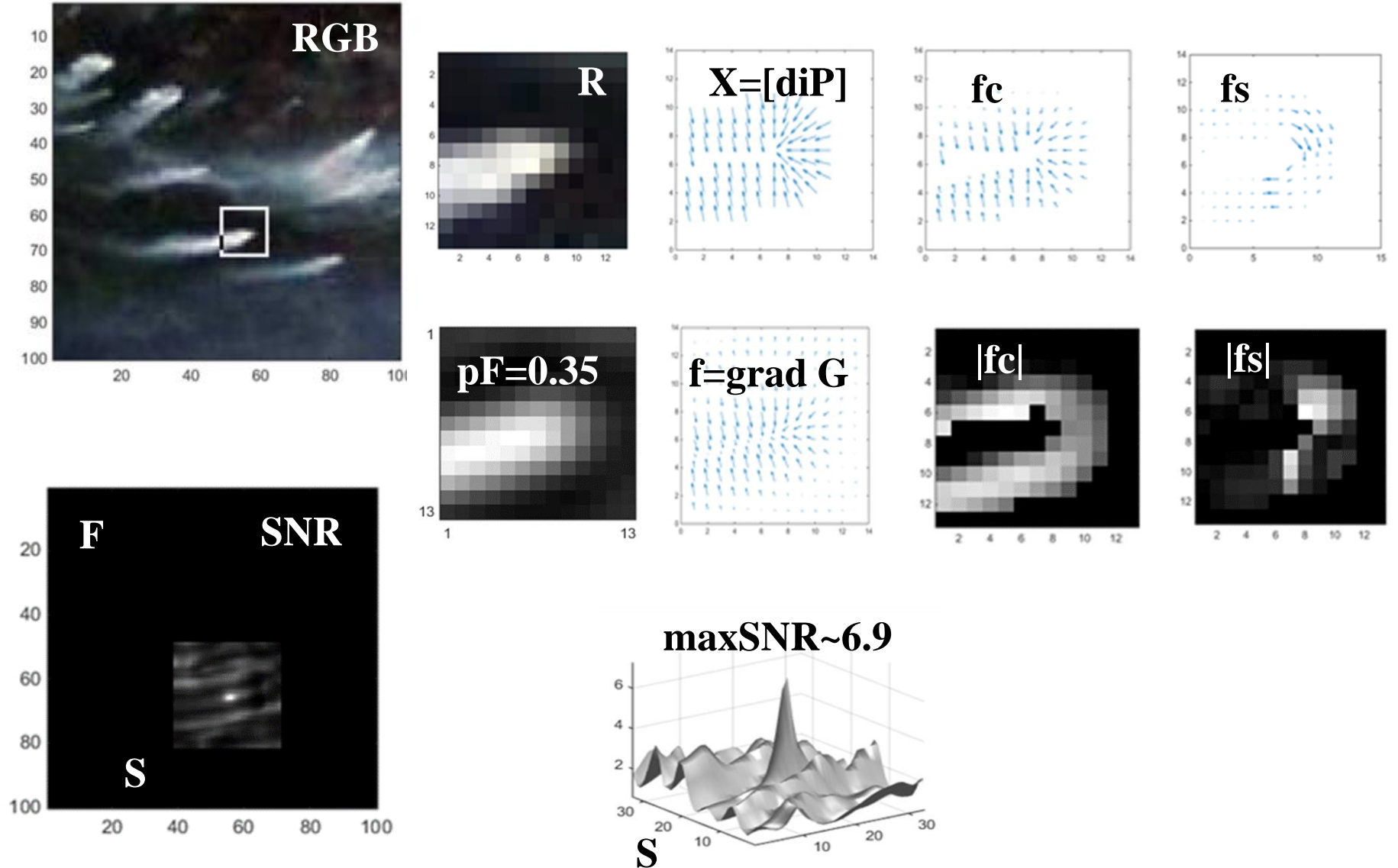


alfa=-18°,  
beta=-41°

alfa=+18°,  
beta=+41°



# Localization of fires with smoke plumes in remote sensing





# Conclusions

1. The ability to accurately assess the position of the Traffic Signs opens up new ways in solving the problem of semantic analysis of images such as “reading Traffic Signs” by the **Navigator robot**.
2. Assessing the exact distance between the Eye Pupils makes it possible to formulate new semantic tasks in evaluating parameters of the “Facial Features” type for implementing **facial image recognition methods**.
3. The plans of the problem of estimating the parameters of vortices in space images of the Earth with remote monitoring.
4. Our plans are to apply field theory operations in the analysis of neoplasms such as tumors, ulcers, metastases, etc. on 3D data in tomography.
5. Possible wide applications GMM in the production of processors.

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